

## **THERMODYNAMIC INVESTIGATIONS IN THE Bi–O SYSTEM\***

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### **Abstract**

With the use of various calculation methods, unknown thermodynamic properties (TP) of Bi<sub>2</sub>O<sub>5</sub> and BiO<sub>2</sub>, as well as the temperature dependencies of reduced Gibbs energy (TDRGE) were determined. With the help of thermodynamic simulation (TS) methods at 300–1500 K, common  $P=10^5$  Pa the thermal decompositions of condensed Bi<sub>2</sub>O<sub>5</sub>, BiO<sub>2</sub>, Bi<sub>2</sub>O<sub>3</sub> and BiO have been investigated in initial atmosphere of O<sub>2</sub> and Ar. Every condensed substance was presented as the individual phase.

It was found that Bi<sub>x</sub>O<sub>y</sub> oxides have temperature stability fields and also districts of possible mixture formation. During equilibrium heating of Bi<sub>x</sub>O<sub>y</sub> oxides the various types of phase transformations were observed. The characteristics of some transformations were estimated.

**Keywords:** decomposition, mixture, oxide, phase transformation, standard enthalpy of formation, thermodynamic simulation

### **Introduction**

According to [1–4] in the Bi–O system condensed oxides BiO, Bi<sub>2</sub>O<sub>3</sub>, BiO<sub>2</sub> and Bi<sub>2</sub>O<sub>5</sub> can exist. The thermodynamic properties (TP) and temperature dependencies of the reduced Gibbs energy (TDRGE) for BiO and Bi<sub>2</sub>O<sub>3</sub> are known, and introduced into the databases IVTANTERMO and ASTRA.BAS [5]. For others oxides the known TP are presented in Table 1. It is clear, that those TP are not enough for calculation of the TDRGE of Bi<sub>2</sub>O<sub>5</sub> and BiO<sub>2</sub>.

The lack of and TDRGE for the above mentioned oxides does not permit reliable thermodynamic investigations into the systems containing bismuth and oxygen (high temperature superconductors, phases with ‘fast ionic transport’ [6, 7] and so on). As a rule, in published works (for example [6–10]) only the properties of condensed Bi<sub>2</sub>O<sub>3</sub> are taken into account. According to above mentioned references, this oxide is the most stable in the Bi–O system. The data about temperature dependencies of partial pressures of gaseous components over Bi<sub>2</sub>O<sub>3</sub> are known and summarized in [11]. But

\* Dedicated to Prof. Šesták in recognition of his outstanding activity in thermal analysis

**Table 1** Thermochemical properties and thermodynamic functions (TDRGE) for Bi<sub>2</sub>O<sub>3</sub> and BiO<sub>2</sub>

Oxide	$\Delta H_{298}^{\circ}/$ kJ mol <sup>-1</sup>	$S_{298}^{\circ}/$ J K <sup>-1</sup> mol <sup>-1</sup>	$H_{298}^{\circ} - H_0^{\circ}/$ J mol <sup>-1</sup>	$T_{\text{decomposition}}/$ K	$a^*$	$b^*$	$c^*$	$C_p$ at $T > T_{\text{tr}}/$ J K <sup>-1</sup> mol <sup>-1</sup>
Bi <sub>2</sub> O <sub>5</sub>	-185[13] -728.1	139.3±10.8	23230	423[3]	161.16	15.978	45.979	142.22
BiO <sub>2</sub>	-335.2	74.3±7.7	11784	573[3] 538[2] 578[1]	69.07	13.432	3.700	75.60
	$T/K$	Coefficients $q_i$ in equation $\Phi^*(T) = q_1 + q_2 \lg x + q_3 x^{-2} + q_4 x^{-1} + q_5 x + q_6 x^2 + q_7 x^3$						
		$q_1$	$q_2$	$q_3$	$q_4$	$q_5$	$q_6$	$q_7$
Bi <sub>2</sub> O <sub>5</sub>	298–423	121.548	38.5001	-0.00549424	0.977894	19.085	0	0
	423–6000	116.468	33.986	0	0.493134	0	0	0
BiO <sub>2</sub>	298–573	57.7669	16.5001	-0.0004427	0.254093	16.00	0	0
	573–6000	62.6359	18.0601	0	0.275511	0	0	0

\*  $a, b, c$  are coefficients of equation:  $C_p = a + b \cdot 10^{-3} T - c \cdot 10^5 T^{-2} / \text{J K}^{-1} \text{ mol}^{-1}$   
 $\Phi^*(T)$  in cal K<sup>-1</sup> mol<sup>-1</sup> for Bi<sub>2</sub>O<sub>5</sub> and BiO<sub>2</sub> ( $x = 10^{-4} \cdot T/K$ )

we did not find in the available literature the full data about the thermal and thermodynamic stability of condensed  $\text{Bi}_2\text{O}_3$ . For others oxides those characteristics evidently are unknown too.

Therefore the goals of this work were:

- the determination of the unknown TP and TDRGE for condensed  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$ ; introduction of those data into the database ASTRA.OWN [12] for application in computer modeling;
- a study of temperature and composition dependencies of condensed  $\text{BiO}$ ,  $\text{Bi}_2\text{O}_3$ ,  $\text{BiO}_2$  and  $\text{Bi}_2\text{O}_5$  thermal decomposition.

## Methods and procedures

Different calculation methods and procedures (for example [12]) were used for determination of the unknown TP of  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$ . The essence of the main methods are given below, together with the calculation results.

Thermal decomposition of condensed  $\text{Bi}_x\text{O}_y$  was studied with the use of thermodynamic simulation (TS) methodology, which was described in detail in [5, 14, 15]. In the system ' $\text{Bi}_x\text{O}_y + \text{O}_2(\text{Ar})$ ' we take into account the thermodynamic functions of condensed  $\text{Bi}$ ,  $\text{BiO}$ ,  $\text{Bi}_2\text{O}_3$ , gaseous  $\text{Bi}$ ,  $\text{Bi}_2$ ,  $\text{Bi}_3$ ,  $\text{Bi}_4$ ,  $\text{BiO}$ ,  $\text{Bi}_4\text{O}_6$ ,  $\text{O}_2$ ,  $\text{O}$  and  $\text{Ar}$  [5], condensed  $\text{Bi}_2\text{O}_5$ , and  $\text{BiO}_2$  (this work). Every condensed substance was present as an individual phase. The study was carried out from 300 to 1500 K with the steps of 10 to 100 K in initial  $\text{O}_2$  or  $\text{Ar}$  atmosphere, common  $P=10^5$  Pa with the application of program ASTRA.4 [5].

## Determination of the TP and TDRGE for $\text{Bi}_2\text{O}_5$ and $\text{BiO}_2$

$\text{Bi}_2\text{O}_5$

The  $S_{298}^0$  values were calculated:

– from the empirical relation [16]:

$$\log S_{298}^0 \approx 0.875 + 0.725 \log n \quad (1)$$

where  $S_{298}^0$  is in  $[\text{cal mol}^{-1} \text{K}^{-1}]$ ;  $n$  is the number of atoms in the molecule;

– from the equation [17]

$$S_{298}^0 \approx A \log M + B \quad (2)$$

where  $M$  is molecular mass of compound,  $A$  and  $B$  are empirical constants in the row of similar compounds (values of  $S_{298}^0$  for  $\text{As}_2\text{O}_5$  and  $\text{Sb}_2\text{O}_5$  were taken from [18]).

The average value of  $S_{298}^0$  equal to  $139.4 \pm 10.8 \text{ J mol}^{-1} \text{K}^{-1}$  we have taken as reliable.

The value of increment  $H_{298}^0 - H_0^0$  was calculated with the use of equation [19]

$$H_{298}^0 - H_0^0 \approx 204 \bar{S}_{298}^0 \exp\left(-\frac{\bar{S}_{298}^0}{23.5}\right), \text{ cal g-atom}^{-1} \quad (3)$$

where,  $\bar{S}_{298}^0 = S_{298}^0 / n$  and  $n$  is the number of atoms in the molecule.

For determination of the dependence  $C_p(T)$ , first we calculated the  $C_{p,298}^0$  value. For it we used:

– the equation [12]:

$$C_{p,298}^0 \approx A \log M + B \quad (4)$$

where  $M$ ,  $A$  and  $B$  are the same as in Eq. (2). (Values of  $C_{p,298}^0$  for  $\text{As}_2\text{O}_5$  and  $\text{Sb}_2\text{O}_5$  were taken from [18, 20]);

– calculation procedures based on the equations:

$$\begin{aligned} C_{p,298}^0(\text{Bi}_2\text{O}_5) &\approx C_{p,298}^0(\text{Bi}_2\text{O}_3) + 2C_{p,298}^0(\text{O}) \\ C_{p,298}^0(\text{Bi}_2\text{O}_5) &\approx 2C_{p,298}^0(\text{BiO}) + 3C_{p,298}^0(\text{O}) \end{aligned} \quad (5)$$

where  $C_{p,298}^0(\text{Bi}_2\text{O}_3)$  and  $C_{p,298}^0(\text{BiO})$  were taken from the database ASTRA.BAS [5] and

$$C_p(T)(\text{O}) \approx 20.04 + 4.07 \cdot 10^{-3} T - 9.42 \cdot 10^{-5} T^{-2} \quad (6)$$

in  $\text{J mol}^{-1} \text{K}^{-1}$  were taken according to Dr. H. Yokokawa (private communication);

– with the use of the empirical equation [16]

$$C_p(T) \approx (7n+2) - (1.16n-1) \cdot 10^{-3} T^{-1} + (1.333n-66) \cdot 10^3 T^{-2}, \quad (7)$$

in  $\text{cal mol}^{-1} \text{K}^{-1}$ , where  $n$  is the number of atoms in the molecule.

The average value  $C_{p,298}^0(\text{Bi}_2\text{O}_5) = 114.2 \pm 5.6 \text{ J mol}^{-1} \text{K}^{-1}$  was taken as reliable and used for calculation of  $C_p(T)$  using the method, described in [21]. In result we found:

$$C_p(\text{Bi}_2\text{O}_5) \approx 161.161 + 15.978 \cdot 10^{-3} T - 45.979 \cdot 10^{-5} T^{-2}, \text{ J mol}^{-1} \text{K}^{-1} \quad (8)$$

According to [3], the  $\text{Bi}_2\text{O}_5$  decomposition finished at 423 K; the change of enthalpy at this temperature was taken as equal to 0.

### *BiO<sub>2</sub>*

For the estimation of  $S_{298}^0$  values we used: – the Latimere method [12]; – Eq. (1); – comparison of  $S_{298}^0(\text{MO}_2)$  ( $M = \text{Hf, Sb, Pb, W}$ ) on row, period and diagonal of the Periodic System (a variant of the Birkengaimé method [12]); – the additive method:

$$\begin{aligned} S_{298}^0(\text{BiO}_2) &\approx S_{298}^0(\text{Bi}_2\text{O}_3) - S_{298}^0(\text{BiO}), \\ S_{298}^0(\text{BiO}_2) &\approx (S_{298}^0(\text{Bi}_2\text{O}_5) + S_{298}^0(\text{Bi}_2\text{O}_3)) / 4 \end{aligned} \quad (9)$$

The values of  $S_{298}^0$  for  $\text{Bi}_2\text{O}_3$  and  $\text{BiO}$  were taken from the database ASTRA.BAS [5],  $S_{298}^0(\text{Bi}_2\text{O}_5)$  was taken from this work, and the average  $= 74.3 \pm 7.7 \text{ J mol}^{-1} \text{K}^{-1}$  was taken as reliable.

The value of  $H_{298}^0 - H_0^0$  was calculated with the use of Eq. (3).

The values of  $C_{p,298}^0$  and the function  $C_p(T)$  have been determined with the help of procedures described above for  $\text{Bi}_2\text{O}_5$ , and are equal to:

$$C_{p,298}^0(\text{BiO}_2) \approx 68.9 \pm 4.1 \text{ and} \quad (10)$$

$$C_p(\text{BiO}_2) \approx 69.07 + 13.432 \cdot 10^{-3} \cdot T - 3.7 \cdot 10^{-5} \cdot T^{-2}, \text{ J mol}^{-1} \text{K}^{-1}$$

The decomposition temperature of  $\text{BiO}_2$  is 573 K according to [3]; the change of enthalpy at this temperature was taken as equal to 0.

For the determination of standard enthalpies of formation ( $\Delta H_{298}^0$ , SEF) of  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$ , various methods and estimations have been used.

First, we used the approximate ratios

$$\frac{T_{\text{ph.tr}}(\text{Sb}_2\text{O}_5) \cdot \text{SEF}(\text{Sb}_2\text{O}_5)}{T_{\text{ph.tr}}(\text{Bi}_2\text{O}_5) \cdot \text{SEF}(\text{Bi}_2\text{O}_5)} \approx \frac{T_{\text{ph.tr}}(\text{SbO}_2) \cdot \text{SEF}(\text{SbO}_2)}{T_{\text{ph.tr}}(\text{BiO}_2) \cdot \text{SEF}(\text{BiO}_2)}, \quad (11)$$

using known data for  $\text{Sb}_2\text{O}_5$  and  $\text{SbO}_2$  taken from [4, 18, 20], and the estimated SEF values of  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$  were equal to  $-566.4$  and  $-13.4$   $\text{kJ mol}^{-1}$ , respectively.

Then we used the universal linear approximation rules (ULAR) [22] (Fig. 1), and determined SEF values of  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$  equal to  $-615.3$  and  $-307.2$   $\text{kJ mol}^{-1}$ , respectively. These values were calculated from linear regression equations, constructed with the use of known SEF for  $\text{Bi}_2\text{O}_3$  and  $\text{BiO}$  [5]:

left side:

$$H_{\text{at}}^0(j) \approx -307.5X(\text{Bi}), \text{ kJ g-atom}^{-1} \quad (12)$$

right side:

$$H_{\text{at}}^0(j) \approx 205(X(\text{Bi}) - 1), \text{ kJ g-atom}^{-1} \quad (13)$$

In the last stage, we used the agreement procedure (AP) [23] on the supposition that only the SEF values for  $\text{BiO}$  and  $\text{Bi}_2\text{O}_3$  are correct [5].

The SEF values for  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$  oxides were determined to be equal  $-728.1$  and  $-335.2$   $\text{kJ mol}^{-1}$ , respectively.

The agreement procedure [23] allows correction of known, and determination of unknown, SEF values of related inorganic substances by use of the following function:

$$\Psi(j) = \frac{H_{\text{at}}^0(j)}{\phi_j}, \text{ kJ g-atom}^{-1} \text{ sort}^{-1} \quad (14)$$

where we named  $\Psi(j)$  as the 'sort standard enthalpy of formation' (SSEF), for the  $j$ -th relative compound (in our case  $\text{Bi}_x\text{O}_y$ );

$$H_{\text{at}}^0(j) = \frac{\Delta H_{298}^0(j)}{n_j}, \text{ kJ g-atom}^{-1} \quad (15)$$

where  $n_j$  is the number of atoms in a molecule of the compounds;

$$\varphi_j = \left( \frac{x}{y} \right)_j \quad (16)$$

where we named  $\varphi_j$  as the ‘sort’ of the  $j$ -th related compound (in our case for  $\text{Bi}_2\text{O}_5$   $\varphi=2/5=0.4$ ; for  $\text{BiO}_2$   $\varphi=1/2=0.5$ , and so on).

It was found that, for related compounds in definite systems, if the values of SEF were determined correctly, then in the coordinates ‘ $\lg\Psi_j - \varphi_j$ ’ we must observe linear dependencies

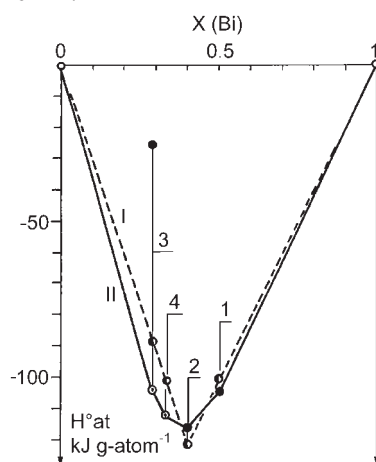
$$\lg\Psi_j \approx A + b\varphi_j \quad (17)$$

In our case

$$\lg\Psi_j = 2.6784 - 0.6584\varphi_j, \text{ kJ g-atom}^{-1} \text{ sort}^{-1} \quad (18)$$

and calculations of SEF for  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$  were made with the use of Eq. (18). Note, that application of the ULAR to analysis of reference data gave an average divergence between calculated and reference data of not more than  $\pm 7.5\%$  [22]; whereas for application of the AP, divergence was not more than  $\pm 2.5\%$  [23].

The results of the various calculations and estimations of SEF values for  $\text{Bi}_x\text{O}_y$  oxides are presented in Table 2. It is seen from Table 2 and Fig. 1, that if we take the SEF for  $\text{Bi}_2\text{O}_3$  and  $\text{BiO}$  [5] as reliable, then the value of the SEF for  $\text{Bi}_2\text{O}_5$  estimated in this work [13] is not correct. We thus take as reliable the SEF for  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$  calculated with the use of the AP.



**Fig. 1** The results of the use of universal linear approximation rules – ULAR [22] (curve 1) and AP [23] (curve 2) for the determination of  $H_{\text{at}}^0$  for  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$ ; 1–4 –  $H_{\text{at}}^0$  for  $\text{BiO}$ ,  $\text{Bi}_2\text{O}_3$ ,  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$ ; • – 1 and 2 –  $H_{\text{at}}^0$  for  $\text{BiO}$  and  $\text{Bi}_2\text{O}_3$  according to [5]; • – 3 – for  $\text{Bi}_2\text{O}_5$  according to [13]; o –  $H_{\text{at}}^0$  for  $\text{Bi}_x\text{O}_y$  according to the ULAR; o –  $H_{\text{at}}^0$  for  $\text{Bi}_x\text{O}_y$  according to the AP

**Table 2** Known data and results of the estimation and calculation of SEF for bismuth oxides

Oxide	$\Delta H_{298}^0/\text{kJ mol}^{-1}$ known data	$\Delta H_{\text{sef}}^0/\text{kJ g-atom}^{-1}$				$\Delta H_{298}^0/\text{kJ mol}^{-1}$ taken as reliable
		known data	estimation on Eq. (11)	on ULAR, Eqs (12), (13)	on AP Eq. (18)	
BiO	-209.4*	-104.7*	-	-102.5	-104.7	-209.4
Bi <sub>2</sub> O <sub>3</sub>	-578.3*	-115.7*	-	-123.0	-115.7	-578.3
Bi <sub>2</sub> O <sub>5</sub>	-185**	-26.43**	-80.9	-87.9	-104.7	-728.1
BiO <sub>2</sub>	-	-	-71.1	-102.4	-111.7	-335.2

\* – according to [5];  
\*\* – according to [13]

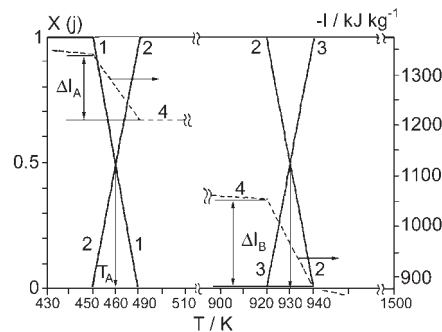
**Table 3** Mole fraction of Bi<sub>2</sub>O<sub>3</sub>

A – in mixtures of BiO <sub>2</sub> +Bi <sub>2</sub> O <sub>3</sub> (initial system BiO <sub>2</sub> +Ar)									
T/K	400	500	600	700	800	820	840	860	880
X(Bi <sub>2</sub> O <sub>3</sub> )	1.284·10 <sup>-12</sup>	6.536·10 <sup>-8</sup>	8.143·10 <sup>-5</sup>	1.247·10 <sup>-2</sup>	5.806·10 <sup>-2</sup>	1.196·10 <sup>-1</sup>	2.60·10 <sup>-1</sup>	6.74·10 <sup>-1</sup>	1.0
B – in mixtures of Bi+Bi <sub>2</sub> O <sub>3</sub> (initial system BiO+Ar, 300–1220 K)									
T/K	600	700	800	900	1000	1100	1200	1220	
X(Bi <sub>2</sub> O <sub>3</sub> )	1.962·10 <sup>-15</sup>	2.815·10 <sup>-12</sup>	7.58·10 <sup>-10</sup>	6.198·10 <sup>-8</sup>	2.256·10 <sup>-6</sup>	7.64·10 <sup>-5</sup>	1.995·10 <sup>-3</sup>	3.35·10 <sup>-3</sup>	
C – in mixtures of Bi+Bi <sub>2</sub> O <sub>3</sub> (initial system BiO+Ar, 1240–1500 K)									
T/K	1240	1260	1280	1300	1320	1340	1400	1500	
X(Bi <sub>2</sub> O <sub>3</sub> )	0.5035	0.5047	0.5060	0.5080	0.5105	0.5140	0.5287	0.5970	

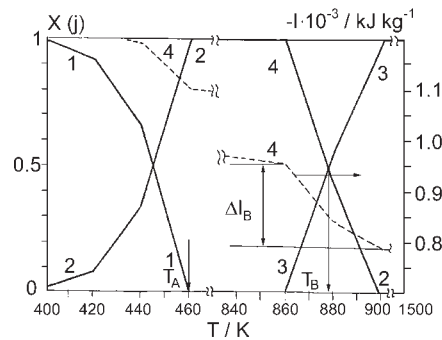
All the properties for  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$  that are taken as reliable are presented in Table 1. They were used for the determination of the TDRGE values for those oxides with the help of the subprogram TERMOS [5]. The numerical coefficients of the approximating polynomials of the TDRGE are given in the second part of Table 1.

### The thermal decompositions of $\text{BiO}$ , $\text{Bi}_2\text{O}_3$ , $\text{BiO}_2$ and $\text{Bi}_2\text{O}_5$

Some results of investigations are presented in Figs 2 to 5 and in Tables 3 to 5.



**Fig. 2** The systems  $\text{Bi}_x\text{O}_y + \text{O}_2$ ; Changes of compositions and energetic characteristics in the interval 450–1500 K; 1–3 –  $X(\text{Bi}_2\text{O}_5)$ ,  $X(\text{BiO}_2)$  and  $X(\text{Bi}_2\text{O}_3)$ ; 4 – changes of systems enthalpies ( $I=f(T)$ );  $T_A$  and  $T_B$ ,  $\Delta I_A$  and  $\Delta I_B$  are the temperatures of the transformations in Eqs (19) and (20), and the changes of system enthalpies near  $T_A$  and  $T_B$ , respectively

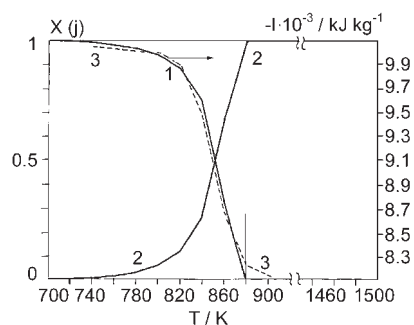


**Fig. 3** The system  $\text{Bi}_2\text{O}_5 + \text{Ar}$ ; Changes of compositions and energetic characteristics in the interval 400–1500 K; 1–3 –  $X(\text{Bi}_2\text{O}_5)$ ,  $X(\text{BiO}_2)$  and  $X(\text{Bi}_2\text{O}_3)$ ; 4 –  $I=f(T)$ ;  $T_A \approx 460$  K is the temperature at the end of phase  $\text{BiO}_2$  formation;  $T_B \approx 880$  K – the same for the  $\text{Bi}_2\text{O}_3$  phase

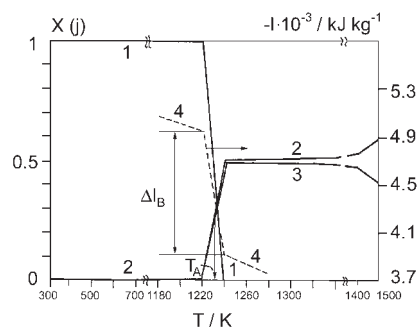
#### The equilibrium heating of $\text{Bi}_x\text{O}_y$ in $\text{O}_2$ (Fig. 2, Table 4)

In surplus oxygen (the initial content of  $\text{O}_2$  in every system was equal to 14 mass%) oxides  $\text{BiO}$ ,  $\text{Bi}_2\text{O}_3$  and  $\text{BiO}_2$  are transformed into  $\text{Bi}_2\text{O}_5$  by 300 K. This phase existed





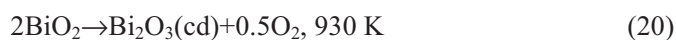
**Fig. 4** The system  $\text{BiO}_2+\text{Ar}$ ; Changes of compositions and energetic characteristics in the interval 700–1500 K; 1 and 2 –  $X(\text{BiO}_2)$  and  $X(\text{Bi}_2\text{O}_3)$ ; 3 –  $I=f(T)$ ;  $T_A \cong 880$  K is the temperature at the end of phase  $\text{Bi}_2\text{O}_3$  formation



**Fig. 5** The system  $\text{BiO}+\text{Ar}$ ; Changes of compositions and energetic characteristics in the interval 300–1500 K; 1–3 –  $X(\text{BiO})$ ,  $X(\text{Bi}_2\text{O}_3)$  and  $X(\text{Bi})$ ; 4 –  $I=f(T)$ ;  $T_A \cong 1230$  K and  $\Delta I_A$  are the temperature of phase transformation and the change of system enthalpy nearly  $T_A$

up to 480 K. Between 480 and 930 K the phase  $\text{BiO}_2$  and at  $T > 930$  K the phase  $\text{Bi}_2\text{O}_3$  were observed.

The sequence of phase composition changes of the oxides can be connected with the transformations:



*The equilibrium heating of  $\text{Bi}_x\text{O}_y$  in Ar (Fig. 3 to 5, Tables 3 and 4)*

Every bismuth oxide under these conditions (initial content of Ar was equal to 14 mass%) has its own type of decomposition.

*Bi<sub>2</sub>O<sub>5</sub>+Ar (Fig. 3, Table 4)*

In the interval 300 to 460 K the condensed phases Bi<sub>2</sub>O<sub>5</sub> and BiO<sub>2</sub> can coexist. The mole fraction of BiO<sub>2</sub> in the mixture, –  $X(\text{BiO}_2)$ , – with rise of temperature increase to:

<i>T</i> /K	300	400	420	440	460
$X(\text{BiO}_2)$	$9.984 \cdot 10^{-7}$	$1.392 \cdot 10^{-2}$	$7.757 \cdot 10^{-2}$	$3.427 \cdot 10^{-1}$	1.0

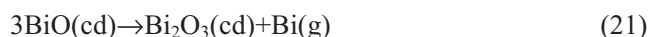
Between 460 and 880 K the lone condensed phase in system is BiO<sub>2</sub>, and at  $T > 880$  K it is Bi<sub>2</sub>O<sub>3</sub>. Consequently, in contrast with the Bi<sub>2</sub>O<sub>5</sub>+O<sub>2</sub> system, an initial phase of Bi<sub>2</sub>O<sub>5</sub> in Ar can exist only with a mixture of phase BiO<sub>2</sub>; the temperature range of existence for the individual phase BiO<sub>2</sub> moves to the low temperature side. These differences are natural results of the atmosphere change and are easily explained.

*BiO<sub>2</sub> + Ar (Fig. 4, Tables 3A and 4)*

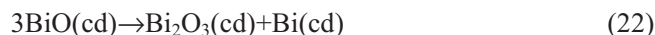
The phases BiO<sub>2</sub> and Bi<sub>2</sub>O<sub>3</sub> can coexist at 300–880 K, and a rise of temperature is accompanied by an increasing  $X(\text{BiO}_2)$  in a mixture of phases (Table 3A). At  $T > 880$  K sesquioxide of bismuth is the lone condensed phase in the system.

*BiO+Ar (Fig. 5, Tables 3B,C and 4)*

Between 300 and 1230 K, a rise of temperature in a mixture of BiO + Bi<sub>2</sub>O<sub>3</sub> resulted in an increase of  $X(\text{BiO}_2)$  from  $\sim 1 \cdot 10^{-18}$  (300 K) to  $\sim 3.35 \cdot 10^{-3}$  (1230 K) (Table 3B). A possible reason for it is disproportion of part of the ‘mother’ phase



Between 1240 and 500 K, the coexisting phases Bi<sub>2</sub>O<sub>3</sub> and Bi were observed as a result of the possible transformation:



at about 1230 K (Table 3C). A decrease of the metallic bismuth content in the mixture Bi<sub>2</sub>O<sub>3</sub>+Bi with rise of temperature can be explained by bismuth evaporation.

*Bi<sub>2</sub>O<sub>3</sub>+Ar*

Over all temperature intervals this oxide is practically the lone condensed phase. Only between 300 and 500 K we observed the existence of BiO<sub>2</sub>, ( $X(\text{BiO}_2)$  in the mixture Bi<sub>2</sub>O<sub>3</sub>+BiO<sub>2</sub> being equal to  $\sim 3.3 \cdot 10^{-6}$ ).

In Table 4, the composition and temperature intervals of existence of the phases are summarized, and the  $T$  and  $\Delta H$  values of some of the phase transformations are given. The last mentioned characteristics were determined according to the methods described in [14, 15]. Let us remember that in the temperature range of a phase transformation, the full enthalpy of system ( $\Delta I$ ) changes by a leap ( $\Delta I$ , Fig. 2 to 5). Because we can calculate numerically by computer experiments not only the function  $I=f(T)$ , but also the molar content of every condensed phase (and gaseous component

**Table 4** Temperature ranges of existence of oxides and characteristics of some phase transformations during equilibrium heating of bismuth oxides

Bi <sub>x</sub> O <sub>y</sub> + O <sub>2</sub>				
300–480 K	480 K	480–930 K	930 K	930–1500 K
Bi <sub>2</sub> O <sub>5</sub>	Bi <sub>2</sub> O <sub>5</sub> →2BiO <sub>2</sub> +0.5O <sub>2</sub> ΔH≈66.5 kJ mol <sup>-1</sup> Bi <sub>2</sub> O <sub>5</sub> ΔH≈32.9 kJ mol <sup>-1</sup> BiO <sub>2</sub>	BiO <sub>2</sub>	2BiO <sub>2</sub> →Bi <sub>2</sub> O <sub>3</sub> +0.5O <sub>2</sub> ΔH≈45.9 kJ mol <sup>-1</sup> BiO <sub>2</sub> ΔH≈91.8 kJ mol <sup>-1</sup> Bi <sub>2</sub> O <sub>3</sub>	Bi <sub>2</sub> O <sub>3</sub>
Bi <sub>2</sub> O <sub>5</sub> + Ar				
360–460 K	460–880 K	880 K	880–1500 K	
Mixture Bi <sub>2</sub> O <sub>5</sub> +BiO <sub>2</sub>	BiO <sub>2</sub>	2BiO <sub>2</sub> →Bi <sub>2</sub> O <sub>3</sub> +0.5O <sub>2</sub> ΔH≈48 kJ mol <sup>-1</sup> BiO <sub>2</sub> ΔH≈96 kJ mol <sup>-1</sup> Bi <sub>2</sub> O <sub>3</sub>	Bi <sub>2</sub> O <sub>3</sub>	–
Bi <sub>2</sub> O <sub>3</sub> + Ar				
300–500 K	500–1500 K			
Mixture Bi <sub>2</sub> O <sub>3</sub> +BiO <sub>2</sub> χ(BiO <sub>2</sub> )=6·10 <sup>-7</sup>	Bi <sub>2</sub> O <sub>3</sub>	–	–	–
BiO <sub>2</sub> + Ar				
300–880 K	880–1500 K			
Mixture Bi <sub>2</sub> O <sub>3</sub> +BiO <sub>2</sub>	Bi <sub>2</sub> O <sub>3</sub>	–	–	–
BiO + Ar				
300–1230 K	1230 K			
Mixture BiO+Bi <sub>2</sub> O <sub>3</sub>	3BiO→Bi <sub>2</sub> O <sub>3</sub> +0.5Bi ΔH≈25.7 kJ mol <sup>-1</sup> BiO ΔH≈38.4 kJ mol <sup>-1</sup> mixture Bi+Bi <sub>2</sub> O <sub>3</sub>	–	–	–

also) at every temperature, we can determine  $\Delta H$  for the phase transformation from the equation

$$\Delta H \approx \frac{\Delta I}{m_T}, \text{ kJ mol}^{-1} \quad (23)$$

where  $m_T$  is the number of moles of the  $j$ -th substance below the phase transformation temperature, or the number of moles of phase transformation products at the temperature of its completion.

## Discussion

Before interpreting these results, we must note a few important initial conditions and assumptions that we used.

(i). We take as reliable the TP and TDRGE for condensed BiO and Bi<sub>2</sub>O<sub>3</sub> from the data base ASTRA.BAS [5]. With the application of the SEF of BiO and Bi<sub>2</sub>O<sub>3</sub>, and assuming that in the Bi-O system can exist the thermodynamically stable phases Bi<sub>2</sub>O<sub>5</sub> and BiO<sub>2</sub>, we calculated, with the use of AP [23], the most important properties, – SEF, – for those oxides. Consequently, if the SEF for BiO and Bi<sub>2</sub>O<sub>3</sub> [5] are not correct, we have used only agreed values of the SEF for Bi<sub>x</sub>O<sub>y</sub> oxides. An independent analysis with the use of a ‘rough’ approximation (Eq. (11)) and the ULAR [22] (Fig. 1) gives us the definite assurance, that the SEF values of Bi<sub>x</sub>O<sub>y</sub> oxides are determined more-or-less correctly. But, for ‘full’ assurance, it is necessary to measure the SEF for Bi<sub>x</sub>O<sub>y</sub> oxides in precise experiments, as well as the other thermochemical properties.

(ii). For the study of the Bi<sub>x</sub>O<sub>y</sub> thermal decomposition, we used the assumption that every condensed compound can be present as an individual phase. This assumption was made for the determination of the principal behaviours of the bismuth oxide and, of course, is only a preliminary and ‘ideal’ point of view on the objects of this investigation.

The following speculations must be reasonable if we take into account the above mentioned notes.

Under the chosen conditions of computer experiments we can conclude, that, in the Bi-O (Ar) systems between 300 and 1500 K, the individual oxides Bi<sub>2</sub>O<sub>5</sub>, BiO<sub>2</sub>, Bi<sub>2</sub>O<sub>3</sub>, BiO as well as the mixtures Bi<sub>2</sub>O<sub>5</sub>+BiO<sub>2</sub>, Bi<sub>2</sub>O<sub>3</sub>+BiO<sub>2</sub>, BiO+ Bi<sub>2</sub>O<sub>3</sub> and Bi<sub>2</sub>O<sub>3</sub>+Bi, can exist.

In atmospheres with surplus O<sub>2</sub>, all initial oxides would be oxidized at 300 K up to the ‘highest’ oxide Bi<sub>2</sub>O<sub>5</sub>, and with increasing temperature, the degree of bismuth oxidation changes from +5→+4→+3.

In an inert gaseous atmosphere, there is also a common tendency of lowering of the average degree of the bismuth oxidation with increasing temperature, but it is accompanied by formation of oxide and oxide–bismuth mixtures over definite temperature intervals.

Under the chosen conditions, the oxide  $\text{Bi}_2\text{O}_3$  is most stable, but not the oxide  $\text{BiO}$ , as would be expected if the results of thermal decomposition investigations of many oxides of less-common metals [4, 5, 11, 14, 15] are taken into account. But at the same time, the results of our study agree with well known experimental facts (see for examples [1–4, 9–11], that the oxide  $\text{Bi}_2\text{O}_3$  is the most stable oxide in the Bi–O system.

The values of the partial pressures of  $\text{O}_2$ , Bi and  $\text{Bi}_4\text{O}_6$  calculated during the TS of thermal decomposition of  $\text{Bi}_2\text{O}_3(\text{cd})$  in inert atmosphere agree satisfactorily with experimental data [11] (Table 5).

**Table 5** Comparison of calculated partial components pressures over  $\text{Bi}_2\text{O}_3$  with experimental data [11] (in MPa)

$T/\text{K}$	$P(\text{O}_2)$		$P(\text{Bi})$		$P(\text{Bi}_4\text{O}_6)$	
	calc.	[11]	calc.	[11]	calc.	[11]
900	$4.27 \cdot 10^{-9}$	$4.59 \cdot 10^{-10}$	$1.47 \cdot 10^{-11}$	$6.10 \cdot 10^{-10}$	$8.10 \cdot 10^{-11}$	$8.97 \cdot 10^{-11}$
1000	$8.71 \cdot 10^{-9}$	$1.55 \cdot 10^{-8}$	$5.71 \cdot 10^{-9}$	$2.04 \cdot 10^{-8}$	$5.20 \cdot 10^{-9}$	$5.26 \cdot 10^{-9}$

This work is probably the first investigation of the thermal stability of bismuth oxides over a wide temperature interval and under different gas atmospheres. Therefore we cannot compare the results with known data. According to the review in [11] only the partial pressures of some components over  $\text{Bi}_2\text{O}_3(\text{cd})$  were measured at about 900 to 1200 K. However, the results of our study are only a first numerical estimation, as according to [11] in the gas phase over condensed  $\text{Bi}_2\text{O}_3$  together with  $\text{Bi}+\text{Bi}_4$ ,  $\text{BiO}$  and  $\text{Bi}_4\text{O}_6$  (their thermodynamic functions taken into account at the TS) also volatile  $(\text{BiO})_n$ , where  $n=2\div 4$ ,  $\text{Bi}_2\text{O}_3$ ,  $\text{Bi}_4\text{O}_5$ ,  $\text{Bi}_3\text{O}_2$  and  $\text{Bi}_3\text{O}$  can exist. For these substances the thermodynamic functions have not yet been determined.

The majority of these data are new. In our opinion, the most interesting of them is the possibility of formation and coexistence of bismuth oxides with different degrees of oxidation at the same temperature. This observation we interpreted as the mixtures of phases, but we can also interpret it as the formation and existence of phases of changing composition, i.e. solid (or liquid) solutions in which molten and crystalline oxide phases can coexist. But these problems can be solved in special investigations, where we must find (or determine) all temperature boundaries ‘solidus–liquidus’ and use definite solution models.

## Conclusions

With the help of various calculation methods, the unknown TP and TDRGE of  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$  have been determined. The thermal decompositions of  $\text{BiO}$ ,  $\text{Bi}_2\text{O}_3$ ,  $\text{Bi}_2\text{O}_5$  and  $\text{BiO}_2$  have been studied from 300 to 1500 K in initial  $\text{O}_2$  and Ar atmospheres. The compositions of the condensed phases and the consequences and characteristics of some phase transformations were determined.

The results of this investigation agree with known information, about  $\text{Bi}_2\text{O}_3$  behaviour at equilibrium heating. It was found that in the Bi–O(Ar) systems can coexist not only individual oxides, but also bismuth oxides, with different degrees of oxidation.

\* \* \*

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